

# Not For Publication Appendix

## F Derivation of Real Rate Functional

This section derives the real interest rate functional given in Equation (25). We start from the characterization of optimal consumption dynamics contained in the Online Appendix C.1. Namely, we use (C.9) and (C.13) to integrate across all households  $j$ :

$$\begin{aligned} \frac{d}{dt} \int_j c_t(a_j, z_j) dj &= \int_{j:u} \left( \partial_a c_t(a_j, z_j) s_t(a_j, z_j) + \partial_t c_t(a_j, z_j) + \sum_{z' \neq z_j} \lambda_{z_j z'} [c_t(a_j, z') - c_t(a_j, z_j)] \right) dj \\ &\quad + \int_{j:c} \sum_{z' \neq z_j} \lambda_{z_j z'} [c_t(0, z') - c_t(0, z_j)] \end{aligned} \quad (\text{F.1})$$

where the  $d\tilde{N}_j$  terms vanish by the exact law of large numbers (Duffie and Sun, 2007, 2012). The first integral on the right-hand side is over unconstrained households ( $j : u$ ), while the second integral is over constrained households ( $j : c$ ). Note that the above equation must be equal to zero, since  $\int_j c_t(a_j, z_j) dj = 1$ , by market clearing. Dividing by  $u''(c_t(a_j, z_j))$  in (C.7) and using CRRA preferences, we obtain:

$$\begin{aligned} -\frac{1}{\gamma}(\rho - r)c_t(a_j, z_j) &= \sum_{z' \neq z_j} \lambda_{z_j z'} \frac{1}{u''(c_t(a_j, z_j))} [u'(c_t(a_j, z')) - u'(c_t(a_j, z_j))] \\ &\quad + \partial_t c_t(a_j, z_j) + s_t(a_j, z_j) \partial_a c_t(a_j, z_j) \end{aligned} \quad (\text{F.2})$$

Integrating over all unconstrained agents and using (F.1) to substitute for  $\partial_t c_t(a_j, z_j) + s_t(a_j, z_j) \partial_a c_t(a_j, z_j)$  yields

$$\begin{aligned} -\frac{1}{\gamma}(\rho - r) \int_{j:u} c_t(a_j, z_j) dj &= \int_{j:u} \sum_{z' \neq z_j} \lambda_{z_j z'} \frac{1}{u''(c_t(a_j, z_j))} [u'(c_t(a_j, z')) - u'(c_t(a_j, z_j))] dj \\ &\quad - \int_j \sum_{z' \neq z_j} \lambda_{z_j z'} (c_t(a_j, z') - c_t(a_j, z_j)) dj \end{aligned} \quad (\text{F.3})$$

1457 Moreover, constrained agents consume their current income  $z_j$ . Hence, adding and  
 1458 subtracting  $-\frac{1}{\gamma}(\rho - r) \int_{j:c} z_j dj$  to the equation above and rearranging yields an ex-  
 1459 pression for the interest rate:

$$r = \rho + \gamma \frac{\int_{j:u} \sum_{z' \neq z_j} \lambda_{z_j z'} \frac{[u'(c_t(a_j, z')) - u'(c_t(a_j, z_j))]}{u''(c_t(a_j, z_j))} dj - \int_j \sum_{z' \neq z_j} \lambda_{z_j z'} (c_t(a_j, z') - c_t(a_j, z_j)) dj}{1 - \int_{j:c} z_j dj} \quad (\text{F.4})$$

1460 Using CRRA utility, and the fact that  $\lambda_{z_j z_j} - \sum_{z' \neq z_j} \lambda_{z_j z'}$ , we may write the above  
 1461 expression as

$$r = \rho - \frac{\int_{j:u} c(a_j, z_j) \left[ \sum_{z'} \lambda_{z_j z'} \left( \frac{c(a_j, z')}{c(a_j, z_j)} \right)^{-\gamma} \right] dj + \gamma \int_j c(a_j, z_j) \left[ \sum_{z'} \lambda_{z_j z'} \frac{c(a_j, z')}{c(a_j, z_j)} \right] dj}{1 - \int_{j:c} z_j dj} \quad (\text{F.5})$$

1462 Relative to the representative agent economy, the sum differs by two terms: the  
 1463 (i) marginal utility variation due to income risk for unconstrained agents, and (ii)  
 1464 consumption variation due to income risk for both constrained and unconstrained  
 1465 agents, multiplied by the coefficient of relative risk aversion. All of these terms  
 1466 are scaled by one minus the total income holdings of constrained agents (which is  
 1467 trivially less one since aggregate consumption is equal to one). The interest rate can  
 1468 be written as a functional in terms of aggregate states by replacing  $c_t(a_{jt}, z_{jt})$  with  
 1469  $c(\omega_{jt} b_t, z_{jt}, \Omega_t)$ . Equation (25) then follows directly.

## 1470 G Household Problem with Diffusion Process

1471 This section sets up an economy in which income follows a diffusion process. We  
 1472 derive as an auxiliary result that  $r_t < \rho$  for all  $t \geq 0$  in this economy.

1473 Concretely, we assume that household income follows a diffusion process given by

$$dz_{jt} = \mu_z(z_{jt})dt + \sigma_z(z_{jt})dB_{jt} \quad (\text{G.6})$$

1474 where  $B_{jt}$  is adapted Brownian motion, independent across  $j$ , and  $\mu_z(\cdot) : \mathbb{R} \rightarrow \mathbb{R}$   
 1475 and  $\sigma_z(\cdot) : \mathbb{R} \rightarrow \mathbb{R}^+$  are twice-differentiable functions. We further assume that (G.6)  
 1476 admits a stationary distribution. The household problem now satisfies the following

1477 HJB equation:

$$\begin{aligned} \rho V_t(a, z) - \partial_t V_t(a, z) &= \max_c \frac{c^{1-\gamma}}{1-\gamma} + \partial_a V_t(a, z) [r_t a + z - \tau_t(z) - c] \\ &\quad + \mu_z \partial_z V_t(a, z) + \frac{1}{2} \sigma_z^2 \partial_{zz}^2 V_t(a, z), \end{aligned} \quad (\text{G.7})$$

1478 together with the boundary condition  $\partial_a V_t(0, z) \geq (z - \tau_t(z))^{-\gamma}$ . A solution to the  
1479 HJB equation alongside (12) solves the household problem. The associated KFE  
1480 equation is:

$$\partial_t g_t(a, z) = -\partial_a [g_t(a, z) \varsigma_t(a, z)] - \partial_z [\mu_z(z) g_t(a, z)] + \frac{1}{2} \partial_{zz}^2 [\sigma_z^2(z) g_t(a, z)] \quad (\text{G.8})$$

1481 **Expected Consumption Dynamics.** We now derive the expected consumption  
1482 dynamics for unconstrained households. Following exactly the same steps outlined in  
1483 Online Appendix C.1 for the case in which income follows a Poisson process, we can  
1484 derive an Euler equation for unconstrained households:

$$\begin{aligned} (\rho - r_t) u'(c_t(a, z)) &= \mu_z(z) u''(c_t(a, z)) \partial_z c_t(a, z) \\ &\quad + \frac{1}{2} \sigma_z^2(z) (u''(c_t(a, z)) \partial_{zz}^2 c_t(a, z) + u'''(c_t(a, z)) (\partial_z c_t(a, z))^2) \\ &\quad + u''(c_t(a, z)) [\partial_t c_t(a, z) + \varsigma_t(a, z) \partial_a c_t(a, z)] \end{aligned} \quad (\text{G.9})$$

1485 We can also use Ito's lemma on  $c_t(a_{jt}, z_{jt})$  to obtain

$$\begin{aligned} dc_t(a_{jt}, z_{jt}) &= [\partial_t c_t(a_{jt}, z_{jt}) + \varsigma_t(a_{jt}, z_{jt}) \partial_a c_t(a_{jt}, z_{jt})] dt \\ &\quad + [\mu_z(z_{jt}) \partial_z c_t(a_{jt}, z_{jt}) + \frac{1}{2} \sigma_z^2(z_{jt}) \partial_{zz}^2 c_t(a_{jt}, z_{jt})] dt + \sigma_z(z_{jt}) \partial_z c_t(a_{jt}, z_{jt}) dB_{jt} \end{aligned} \quad (\text{G.10})$$

1486 Taking expectations of the above equation, combining it with (G.9), and imposing  
1487 that  $u$  is isoelastic with curvature parameter  $\gamma$  yields the expected consumption dy-  
1488 namics for unconstrained households:

$$\frac{\mathbb{E}_t[dc_{jt}]}{c_{jt} dt} = \frac{1}{\gamma} (r_t - \rho) + \frac{\gamma + 1}{2} \sigma_z^2(z_{jt}) \left( \frac{\partial_z c_t(a_{jt}, z_{jt})}{c_t(a_{jt}, z_{jt})} \right)^2 \quad (\text{G.11})$$

1489 Constrained households simply consume their income. Hence, their consumption  
 1490 dynamics are

$$dc_{jt} = [\mu_z(z_{jt})]dt + \sigma_z(z_{jt})dB_{jt} \quad (\text{G.12})$$

1491 The expected consumption dynamics of constrained households are therefore given  
 1492 by

$$\frac{\mathbb{E}_t[dc_{jt}]}{dt} = \mu_z(z_{jt}) \quad (\text{G.13})$$

**Derivation of Interest Rate Functional.** Integrating over the consumption dynamics of unconstrained households and making use of the fact that

$$\int_j \frac{dc_{jt}}{dt} dj = 0$$

1493 yields

$$\begin{aligned} 0 = & \int_{j:u} \frac{1}{\gamma} (r_t - \rho) c_{jt} dj + \int_{j:u} \frac{(\gamma + 1)}{2} c_t(a_{jt}, z_{jt}) \left( \frac{\sigma_z(z_{jt}) \partial_z c_t(a_{jt}, z_{jt})}{c_t(a_{jt}, z_{jt})} \right)^2 dj \\ & + \int_{j:c} [\mu_z(z_{jt}) c_t(a_{jt}, z_{jt})] dj \end{aligned} \quad (\text{G.14})$$

1494 where we have used (G.11) and (G.13). Finally, imposing market clearing  $\int_j c_{jt} dt = 1$   
 1495 yields

$$r_t = \rho - \frac{\frac{\gamma(\gamma+1)}{2} \int_{j:u} c_t(a_{jt}, z_{jt}) \left( \frac{\sigma_z(z_{jt}) \partial_z c_t(a_{jt}, z_{jt})}{c_t(a_{jt}, z_{jt})} \right)^2 dj + \gamma \int_{j:c} [c_t(a_{jt}, z_{jt}) \mu_z(z_{jt})] dj}{1 - \int_{j:c} z_{jt} dj} \quad (\text{G.15})$$

1496 Note that this implies that  $r_t < \rho$  for all  $t \geq 0$  (not just in steady-state) if no  
 1497 households are constrained, or if  $\int_{j:c} \mu_z(z_{jt}) dj > 0$ , so that constrained households expect  
 1498 their income to increase, on average. We may also write the formula analogously  
 1499 as the one in the main text for the Poisson income process (25):

$$0 = \frac{\mathcal{C}_t^u}{\gamma} (r_t - \rho) + \mathcal{C}_t^u \tilde{\mathbb{E}}_t^u \left[ \frac{\gamma + 1}{2} \sigma_z^2(z) \left( \frac{\partial_z c_t(a, z)}{c_t(a, z)} \right)^2 - \mu_z(z) \right] + \tilde{\mathbb{E}}_t [\mu_z(z)] \quad (\text{G.16})$$

## 1500 H Additional Details on Long-Run Anchoring

1501 In this section, we demonstrate how the monetary authority can eliminate all dynamic  
1502 equilibria that converge to the high inflation steady-state, leaving only a unique equi-  
1503 librium that leads to the saddle-path stable, low-inflation steady-state. Concretely,  
1504 suppose the monetary authority has the power to coordinate private sector beliefs  
1505 about long-run inflation. Under such a setting we envisage two pillars of central bank  
1506 policy: (i) a path or rule for short-term nominal interest rates  $i_t$ , and (ii) a long-run  
1507 inflation target  $\pi^*$ . Whereas the interest rate is a policy tool that the central bank  
1508 directly implements by intervening in appropriate markets or paying interest on re-  
1509 serves, the long-run inflation target is no more than an attempt to coordinate beliefs.  
1510 If:

- 1511 (i) the long-run inflation target and the long-run nominal interest rate ( $\pi^*, i^*$ ) are  
1512 set to be consistent with the equilibrium real rate at the saddle-path steady  
1513 state,  $i^* - \pi^* - g = r_H^*$ ;
- 1514 (ii) fiscal policy follows a constant deficit policy or a passive interest payment re-  
1515 action rule with  $\phi_s < 1$ , so that the high real rate, low inflation steady-state is  
1516 saddle-path stable;
- 1517 (iii) private sector beliefs about long-run inflation are consistent with the central  
1518 bank's target,

1519 then there is a unique real equilibrium and the price-level and inflation are pinned  
1520 down for all  $t$ . The third of these conditions is a big “if”, and there is no fundamental  
1521 reason to expect it to hold. However the key point is that managing *long-run* inflation  
1522 expectations is sufficient to pin down the price level and inflation in the *short-run*.  
1523 If the central bank is successful at convincing the private sector to coordinate on a  
1524 long-run inflation target, then this is sufficient to eliminate any indeterminacy about  
1525 inflation at all points in time. Note that anchoring long-run inflation expectations  
1526 at  $\pi^*$  does not assume away the issue of price-level determination in the short-run.  
1527 Both the initial price level and subsequent inflation remain endogenous and depend  
1528 on monetary policy, fiscal policy and private sector behavior.

1529 Even with long-run inflation anchoring, fiscal policy remains an essential compo-  
1530 nent of price-level determination. Coordinating long-run expectations only uniquely  
1531 determines the price-level in the short-run if fiscal policy acts in a way that ensures

1532 the saddle-path stability of the low-inflation steady state. Such fiscal policy settings  
 1533 are the same as those required for uniqueness in the case with persistent surpluses.

## 1534 I Proof for the Model With Long-Term Debt

1535 **Proposition 5.** *The household budget constraint follows (6) and the real government*  
 1536 *budget constraint follows (18) for  $t > 0$ . Moreover, the price of long-term debt satisfies*  
 1537 *the following differential equation for  $t > 0$ :*

$$\frac{\dot{q}_t}{q_t} + \frac{\chi - \delta q_t}{q_t} = i_t \quad (\text{I.17})$$

*Proof.* We define the auxiliary variable  $u = A_{jt}^l$ . Note that this implies  $dA_{jt}^l = u$ . Hence, the households HJB equation is given by:

$$\begin{aligned} & \tilde{\rho}V_t(A^l, A^s, z) - \partial_t V(A^l, A^s, z) = \\ & \max_{c,u} \frac{c^{1-\gamma}}{1-\gamma} + \tilde{s}_t \partial_{A^s} V_t(A^l, A^s, z) + \partial_{A^l} V_t(A^l, A^s, z)u + \sum_{z' \neq z} \lambda_{zz'} [V_t(A^l, A^s, z') - V_t(A^l, A^s, z)] \end{aligned}$$

where

$$\tilde{s}_t := i_t A^s + (\chi - \delta q_t) A^l + (z - \tau(z)) P_t y_t - P_t \tilde{c}_t - q_t u$$

1538 The first-order condition with respect to  $u$  is given by:

$$q_t \partial_{A^s} V(A^l, A^s, z) = \partial_{A^l} V_t(A^l, A^s, z) \quad (\text{I.18})$$

1539 We may differentiate with respect to time to obtain:

$$q_t \partial_{A^s, t}^2 V_t(A^l, A^s, z) + \partial_t q_t \partial_{A^s} V(A^l, A^s, z) = \partial_{A^l, t} V_t(A^l, A^s, z) \quad (\text{I.19})$$

1540 The envelope condition for the HJB with respect to  $A^l$  is:

$$\tilde{\rho} \partial_{A^l} V_t - \partial_{t, A^l}^2 V_t = \tilde{s}_t \partial_{A^s, A^l}^2 V_t + (\chi - \delta q_t) \partial_{A^l} V_t + u \partial_{A^l}^2 V_t + \sum_{z' \neq z} \lambda_{zz'} [\partial_{A^l} V_t - \partial_{A^l} V_t] \quad (\text{I.20})$$

1541 Similarly, the envelope condition for the HJB with respect to  $A^s$  is:

$$\tilde{\rho}\partial_{A^s}V_t - \partial_{t,A^s}^2V_t = \tilde{s}_t\partial_{A^s}^2V_t + i_t\partial_{A^s}V_t + u\partial_{A^l,A^s}^2V_t + \sum_{z' \neq z} \lambda_{zz'}[\partial_{A^s}V_t - \partial_{A^s}V_t] \quad (\text{I.21})$$

1542 Multiplying (I.21) by  $q_t$ , subtracting Equation (I.20) from (I.21) and using (I.18) and  
 1543 (I.19) yields:

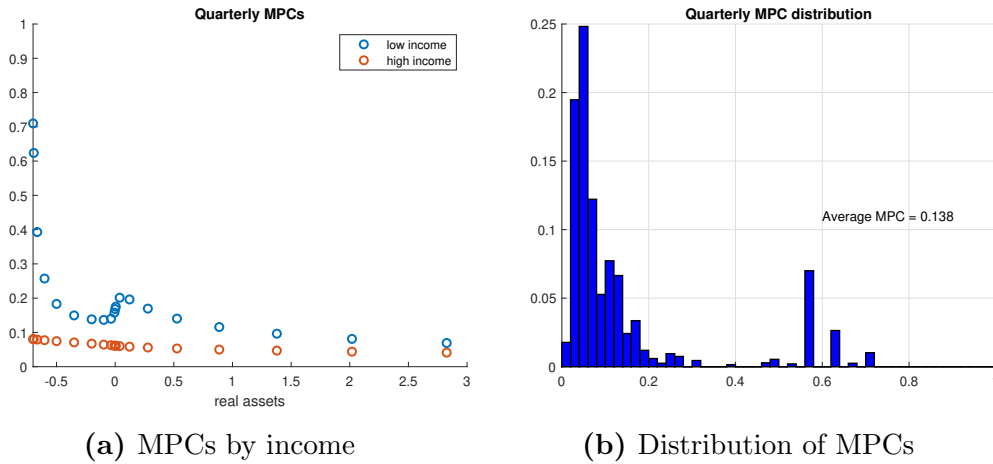
$$(q_t i_t - (\chi - \delta q_t) - \partial_t q_t)\partial_{A^l}V_t = 0 \quad (\text{I.22})$$

1544 By market clearing, we must have  $\partial_{A^l}V_t > 0$  (otherwise no long-term debt would be  
 1545 purchased in equilibrium). Hence, we have the arbitrage relationship:

$$\frac{\dot{q}_t}{q_t} + \frac{\chi - \delta q_t}{q_t} = i_t \quad (\text{I.23})$$

1546 Differentiating  $B_t = q_t B_t^l + i_t B_t^s$  and using the (E.57) yields (15), which can be written  
 1547 in real terms. This completes the proof.  $\square$

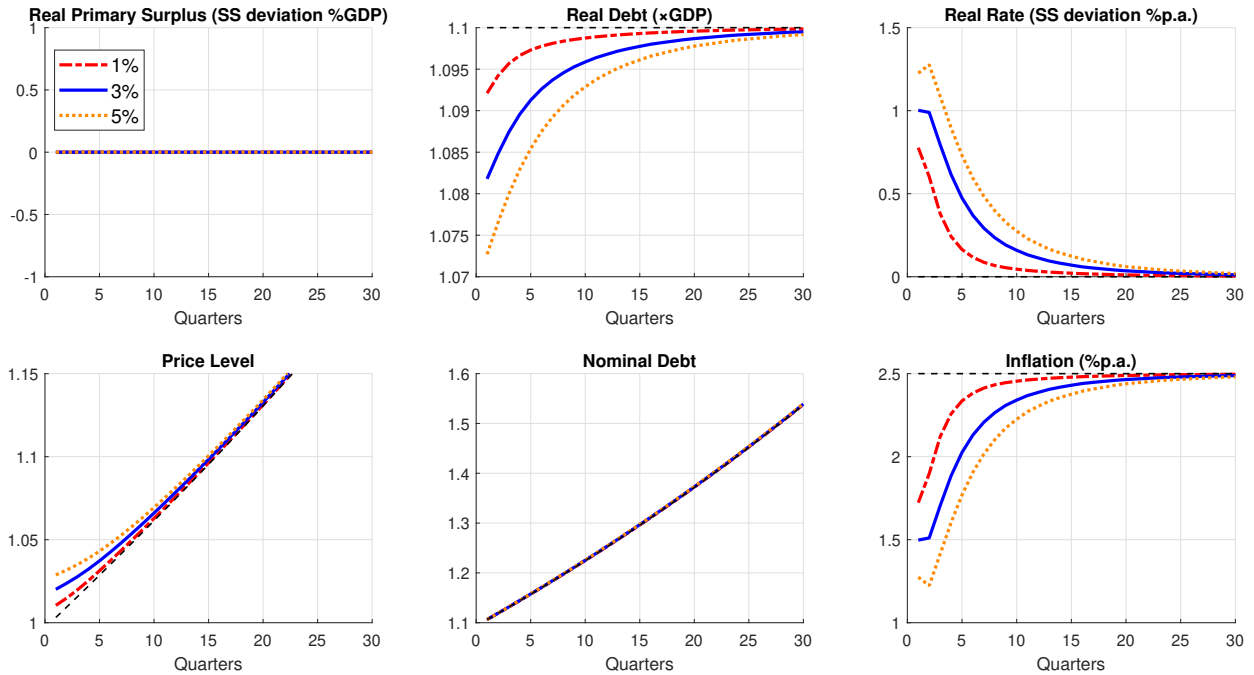
## 1548 J Supplement on Wealth Distribution and MPCs



**Figure 14:** MPCs in the calibrated steady-state

1549 This section provides some additional detail on the MPCs in the calibrated steady-  
 1550 state. Figure 14a shows the dependence of marginal propensities to consume on real  
 1551 assets, disaggregated by the highest and lowest income draws. The plotted MPCs are

Figure 15



*Note:* Impulse responses to a temporary increase in the wealth tax, with the proceedings distributed lump-sum, for various values of the wealth tax. In all experiments, the wealth tax is levied on the top 10% of the wealth distribution, the proceeds of which are redistributed lump-sum to the bottom 60%.

1552 the quarterly marginal propensities to consume from an unanticipated \$500 income  
 1553 gain.

1554 MPCs are not monotonically decreasing in real assets because there is a borrowing  
 1555 wedge. Households with zero assets therefore have a high marginal propensity to  
 1556 consume because of the discontinuous cost of borrowing (Kaplan and Violante, 2014).  
 1557 Note that the MPCs of high income households lie uniformly below the MPCs of low  
 1558 income households.

1559 Figure 14b plots the distribution of MPCs in the calibrated steady-state. A large  
 1560 number of households have an MPC of around 0.15 and hold zero assets. The average  
 1561 MPC in the economy is 0.14, which is in line with commonly estimated values for  
 1562 marginal propensities to consume (Jappelli and Pistaferri, 2010).



## 1563 **K Inflationary Effects of Pure Redistribution**

1564 A comparison of the heterogeneous agent and representative agent economies in the  
1565 preceding experiments suggests that redistribution itself has effects on the price level  
1566 and inflation that are independent of the overall level of surpluses and nominal govern-  
1567 ment debt. To emphasize the inflationary effects of redistribution, Figure 15 shows  
1568 simulations from purely redistributive shocks. We consider one-time wealth taxes  
1569 levied on the top 10% of the wealth distribution, the proceeds of which are redis-  
1570 tributed lump-sum to the bottom 60%. Although these shocks do not entail any new  
1571 issuance of government debt or any change in primary deficits, they do cause a pe-  
1572 riod of inflation. The redistribution causes upward pressure on consumption because  
1573 low-wealth households have higher average MPCs than high wealth households. Equi-  
1574 librium is achieved through a period of higher real interest rates. The corresponding  
1575 lower government revenues require a downward revaluation in real debt through a  
1576 jump in the price level.

1577 **Inflationary Effects of Proportional Wealth Taxes.** We contrast this exper-  
1578 iment with another version of wealth taxation. Consider an economy where the  
1579 government levies a proportional wealth tax at a rate of  $\tau_b$  so that total primary  
1580 surpluses are  $s^* + \tau_b b_t$  (where  $s^*$  are surpluses net of revenue from the wealth tax).  
1581 The real government budget constraint becomes:

$$db_t = [(r_t - \tau_b)b_t - s^*] dt. \quad (\text{K.24})$$

1582 The wealth tax appears in the household budget constraint in a similar fashion, as  
1583 it increases the after-tax real rate paid to the government,  $r_t - \tau_b$ . Changes in  $\tau_b$   
1584 therefore only affect the inflation rate through the Fisher equation, but otherwise  
1585 leave the real economy and the initial price level unchanged.

## 1586 **L Endogenous Output**

1587 In this subsection, we outline an economy in which labor is a variable input in pro-  
1588 duction. Next, we discuss how endogenous output affects price level and inflation  
1589 dynamics in response to unanticipated shocks.

1590 **L.1 Set-Up**

1591 **Households.** The set-up of the household problem closely follows that of the main  
 1592 text. However, we assume that households choose real consumption flows  $\tilde{c}_{jt}$  and  
 1593 hours worked  $\ell_{jt}$  to maximize

$$\mathbb{E}_0 \int e^{-\rho t} \left[ \frac{\tilde{c}_{jt}^{1-\gamma}}{1-\gamma} - \phi_t^{1-\gamma} \frac{\ell_{jt}^{1+\psi}}{1+\psi} \right] dt \quad (\text{L.25})$$

1594 where the expectation is taken with respect to households' efficiency units of labour  
 1595  $z_{jt}$ . The exponent  $\psi > 0$  is the inverse of the Frisch elasticity of labor supply. The  
 1596 term  $\phi_t$  is a time-varying constant that augments the labor disutility in order to  
 1597 allow the economy to be consistent with balanced growth when  $\gamma \neq 1$ . Concretely,  
 1598 we assume that

$$\phi_t = \tilde{\phi} e^{gt} \quad (\text{L.26})$$

1599 where  $\tilde{\phi} > 0$  and  $g > 0$  is the growth rate of the economy. This formulation im-  
 1600 plies that a stationary equilibrium exists. Moreover, the distribution of hours across  
 1601 households is constant in the stationary equilibrium.<sup>42</sup> The households nominal bud-  
 1602 get constraint therefore satisfies

$$dA_{jt} = [i_t A_{jt} + (1 - \tau_{1t}) z_{jt} P_t w_t \ell_{jt} - P_t \tilde{c}_{jt} + P_t \tau_{0t}] dt \quad (\text{L.27})$$

1603 where  $w_t$  is the real wage rate for effective labor services at time  $t$ ,  $\tau_{0t}$  is a lump-sum  
 1604 payment and  $\tau_{1t}$  is a constant proportional tax rate. We assume that  $\tau_{0t}$  grows at a  
 1605 rate  $g > 0$  in order to ensure that a stationary equilibrium exists:

$$\tau_{0t} = \tilde{\tau}_0 e^{gt} \quad (\text{L.28})$$

1606 Finally, the stochastic process for  $z_{jt}$  and the definition of de-trended real variables  
 1607 for the evolution of real debt are identical to those of the main text.

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<sup>42</sup>We intentionally assume separability between hours and consumption in the instantaneous utility function so as to maximize comparability between the economy with endogenous output presented in this subsection and the endowment economy presented in the main text. In particular, the endowment economy can be closely approximated for large  $\psi$  and a given calibrated  $\tilde{\phi}$ . We note, however, that preferences by King et al. (1988) leave the key mechanisms unaffected.

1608 **Firms.** We assume that perfectly competitive firms hire labor to produce output  $y_t$   
 1609 with the constant returns to scale (CRS) production function

$$y_t = \Theta_t L_t \tag{L.29}$$

1610 where  $\Theta_t$  is aggregate total factor productivity that grows at a rate  $g > 0$  and  $L_t$  are  
 1611 total effective hours:

$$L_t := \int_j z_{jt} \ell_{jt} dj \tag{L.30}$$

1612 CRS implies that the real wage rate  $w_t$  is equal to  $\Theta_t$  for all  $t \geq 0$ .

1613 **Government.** The dynamics for government debt are given by

$$dB_t = [i_t B_t - s_t P_t y_t] dt \tag{L.31}$$

1614 where  $s_t$  is the ratio of primary surpluses to output and is determined by the  $\tau_{0t}$  and  
 1615  $\tau_{1t}$  as

$$s_t = \frac{\tau_{0t}}{y_t} + \int_{j \in [0,1]} \tau_{1t} w_t z_{jt} \ell_{jt} dj \tag{L.32}$$

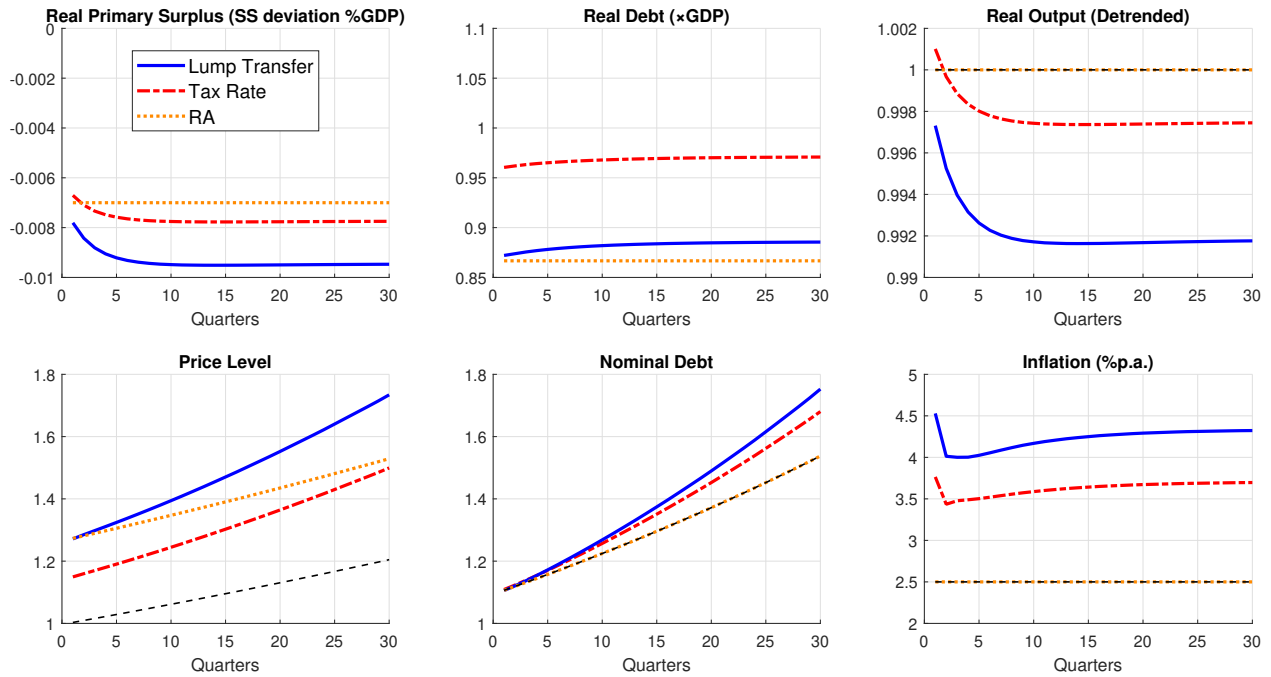
1616 De-trended real government debt then follows

$$db_t = [r_t b_t - s_t] dt \tag{L.33}$$

1617 We do not consider unanticipated changes in the nominal rate in this section. Conse-  
 1618 quently, we assume an interest rate peg  $i_t = i^*$  without loss of generality in analyzing  
 1619 real dynamics.

1620 **Calibration.** Our calibration sets  $\psi = 2$ , so that the intensive-margin Frisch elas-  
 1621 ticity of labor supply is equal to one-half, in line with the recommendation of [Chetty](#)  
 1622 [et al. \(2011\)](#). Moreover, we calibrate  $\tilde{\phi}$  so as to set total hours worked equal to unity.  
 1623 Allowing labor to adjust on the intensive margin provides additional insurance to  
 1624 households. As such, the discount rate increases to 6.1% p.a. (relative to 2.8% p.a.  
 1625 from the calibration in the main text) in order to match a debt-to-annual GDP ratio  
 1626 of 1.10. The values for the remaining parameters remain unchanged from [Table 1](#).

Figure 16



*Note:* Impulse responses to a permanent expansion in primary deficits in the economy with endogenous output. The dotted orange line shows the effects of a permanent reduction in surpluses in the Representative Agent model due to a change in transfers. The solid blue line labelled “Lump Sum” illustrates the dynamics following an expansion of lump sum transfers. The dashed red line labelled “Tax Rate” illustrates the dynamics following a tax cut. In all experiments, deficits increase by 0.7% of pre-shock GDP.

## 1627 L.2 Quantitative Exercise

1628 We consider the economy’s response to an increase in deficits. First, we consider  
 1629 the economy’s response to a permanent change in  $\tilde{\tau}_{0t}$  from 0.333 to 0.340, keeping  $\tau_1$   
 1630 fixed. Second, we consider a permanent change in  $\tau_{1t}$  from 0.300 to 0.307, keeping  
 1631  $\tau_{0t}$  fixed. These changes amount to a change in deficits from 3.3% to 4% of GDP, if  
 1632 output was unchanged (in line with the analysis of Section 5.5).

1633 An increase in deficits due to a tax cut results in a smaller jump in the initial  
 1634 price level, relative to the transfer expansion case. The main reason is that lower  
 1635 taxation increases the labor supply (whereas a transfer expansion lowers it). The  
 1636 corresponding rise in output raises tax revenues and attenuates the long-run increase

1637 in primary deficits relative to the transfer expansion.<sup>43</sup>

1638 In both economies, however, real output eventually *declines* relative to the rep-  
1639 resentative agent benchmark. In order to understand this result, consider the tax  
1640 cut experiment. There are two forces that contribute to an increase in labor supply.  
1641 First, the tax cut directly raises the return to working, as explained above. Second,  
1642 households in the new steady-state hold lower amounts of wealth, on average. This  
1643 gives rise to positive wealth effects that also expands total hours worked. However,  
1644 the new steady-state features a lower long-run real rate – a force only present in the  
1645 heterogeneous agent economy. The reduction in the real rate increases consumption  
1646 state-by-state due to the intertemporal savings motive, thereby reducing total hours  
1647 worked. This last force is sufficiently strong that it counteracts the positive effect on  
1648 output due to the lower tax rate and the change in the wealth distribution. Con-  
1649 sequently, in the long-run output falls and deficits rise relative to the representative  
1650 agent economy.

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<sup>43</sup>The tax cut also increases precautionary motives by amplifying the volatility of post-tax earnings, in line with the reasoning of Section 5.5. The real interest rate therefore decreases relatively less. Since the government now finances its debt at a higher cost, this a force that contributes to a larger initial jump in the price level. However, this mechanism is dominated by labor-supply channel.

## 1651 **References**

- 1652 Chetty, R., Guren, A., Manoli, D., and Weber, A. (2011). Are micro and macro labor  
1653 supply elasticities consistent? A review of evidence on the intensive and extensive  
1654 margins. *American Economic Review*, 101(3):471–475.
- 1655 Duffie, D. and Sun, Y. (2007). Existence of independent random matching. *Annals*  
1656 *of Applied Probability*, 17(1):86–419.
- 1657 Duffie, D. and Sun, Y. (2012). The exact law of large numbers for independent  
1658 random matching. *Journal of Economic Theory*, 147(3):1105–1139.
- 1659 Jappelli, T. and Pistaferri, L. (2010). The consumption response to income changes.  
1660 *Annual Review of Economics*, 2(1):479–506.
- 1661 Kaplan, G. and Violante, G. L. (2014). A model of the consumption response to fiscal  
1662 stimulus payments. *Econometrica*, 82(4):1199–1239.
- 1663 King, R. G., Plosser, C. I., and Rebelo, S. T. (1988). Production, growth and business  
1664 cycles: I. The basic neoclassical model. *Journal of Monetary Economics*, 21(2-  
1665 3):195–232.